

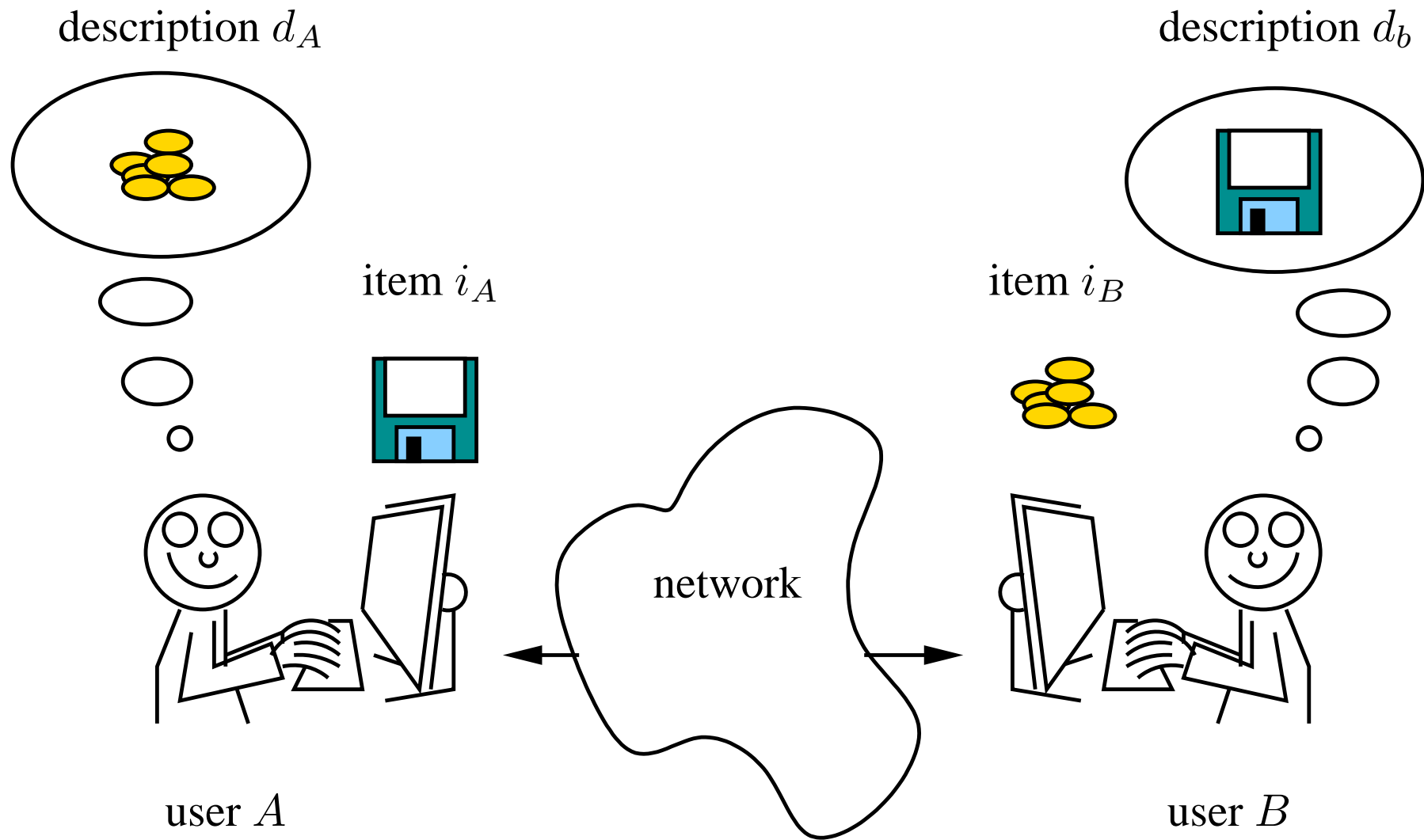
**The Problem of Fair Exchange,  
its Formalization,  
and its Relation to  
other Problems in Distributed Computing**

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based on joint work with  
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See forthcoming article “Fair Exchange” in *The Computer Journal*  
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# Exchanging Goods on the Internet



# Motivation

- Goal: Exchange the items in a **fair** manner.
- Fair exchange is an important notion in e-commerce:
  - Exchanging electronic goods and payment.
  - Digital contract signing.
  - Certified e-mail.
  - Mutual disclosure of identities.
- Assumption: items can be fully validated.

# Outline

- What is fair exchange (more precisely)?
- Some fair exchange protocols and some impossibilities.
- How formalize fairness?
- Relation to transactions and consensus.
- Some research issues.

## Fair Exchange Context

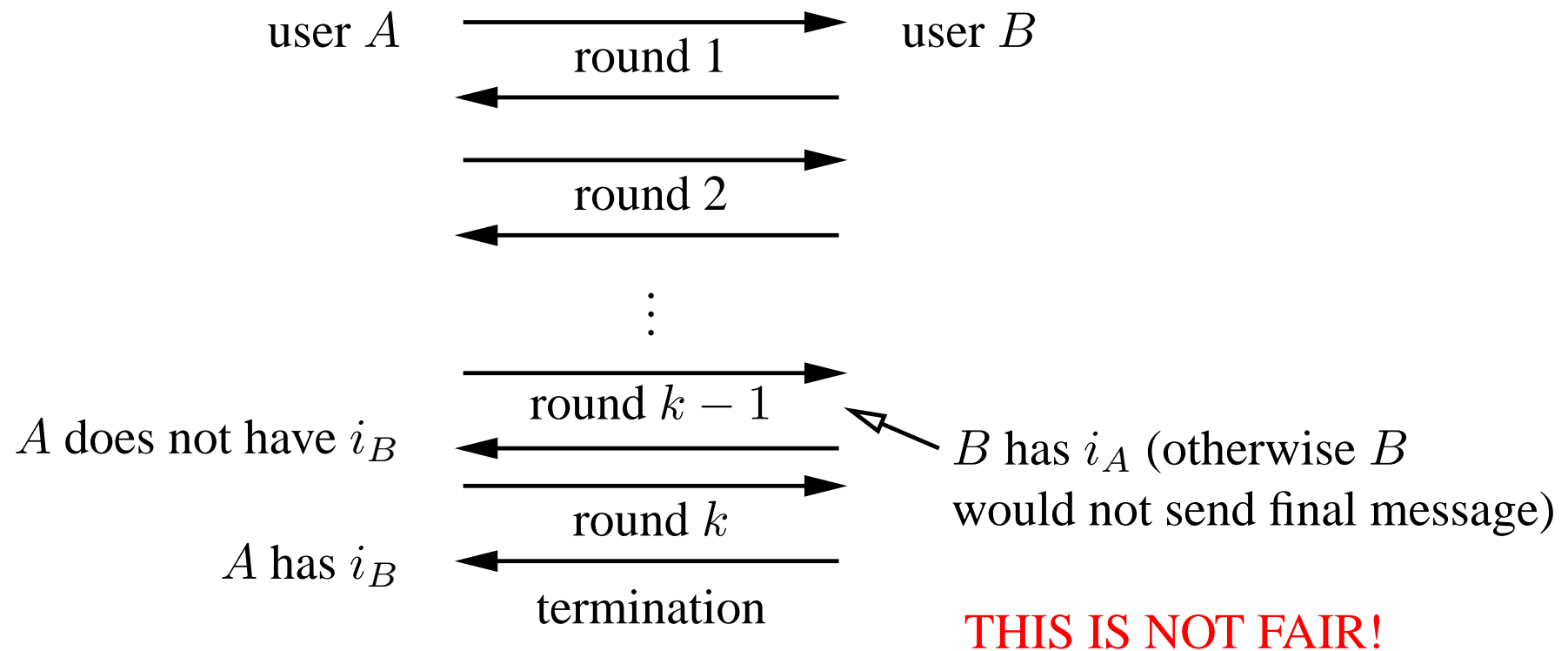
- $A, B, i_A, i_B, d_A$  and  $d_B$  are given.
- System model is asynchronous.
  - Users have a weak notion of timeout: A user can unilaterally decide to **abandon the exchange** (i.e., enforce a termination state for himself).
- Nothing is known about other parties in the system apart from users  $A$  and  $B$  (for now).
- Adversary assumption:
  - At any point in the protocol, a misbehaving user may go silent and not participate in the exchange anymore.
  - More generally: passive Dolev-Yao model [[Dolev and Yao 1983](#)].

## Fair Exchange Properties

- A **protocol solves fair exchange** between two parties  $A$  and  $B$  if it satisfies three conditions:
  - **Effectiveness**:  
If both parties behave according to the protocol, both parties do not want to abandon the exchange, and both items match the description then, when the protocol has completed,  $A$  has  $i_B$  and  $B$  has  $i_A$ .
  - **Termination**:  
A party which behaves according to the protocol will eventually complete the protocol (and know that it has completed)
  - **Fairness** (informal version):  
If at least one party does not behave according to the protocol or if at least one item does not match the description, then no honest participant wins or loses anything valuable.

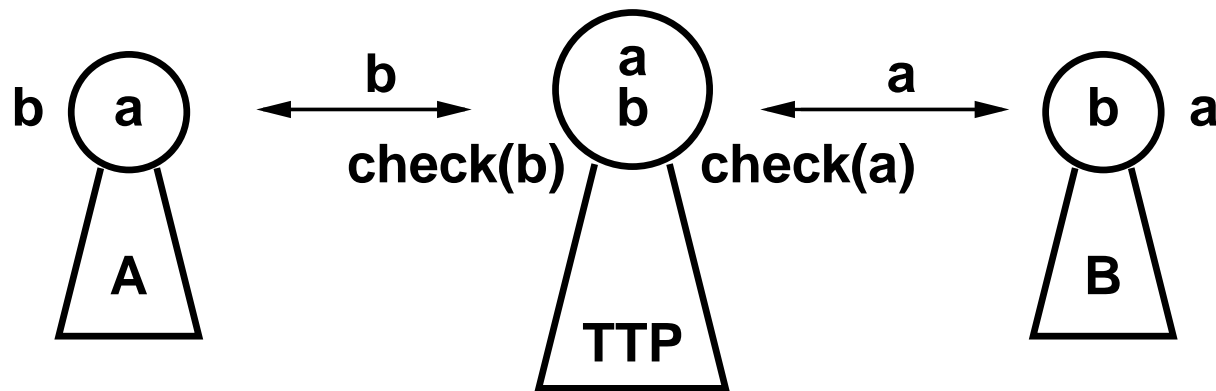
## Two-Party Fair Exchange: Impossibility

- In two-party fair exchange, who should go first?
- Impossibility proof by [Even and Yacobi \[1980\]](#):



## Fair Exchange with an Active Trustee

- Simplest protocol: use an **active trusted third party** (TTP) to perform the exchange. ■



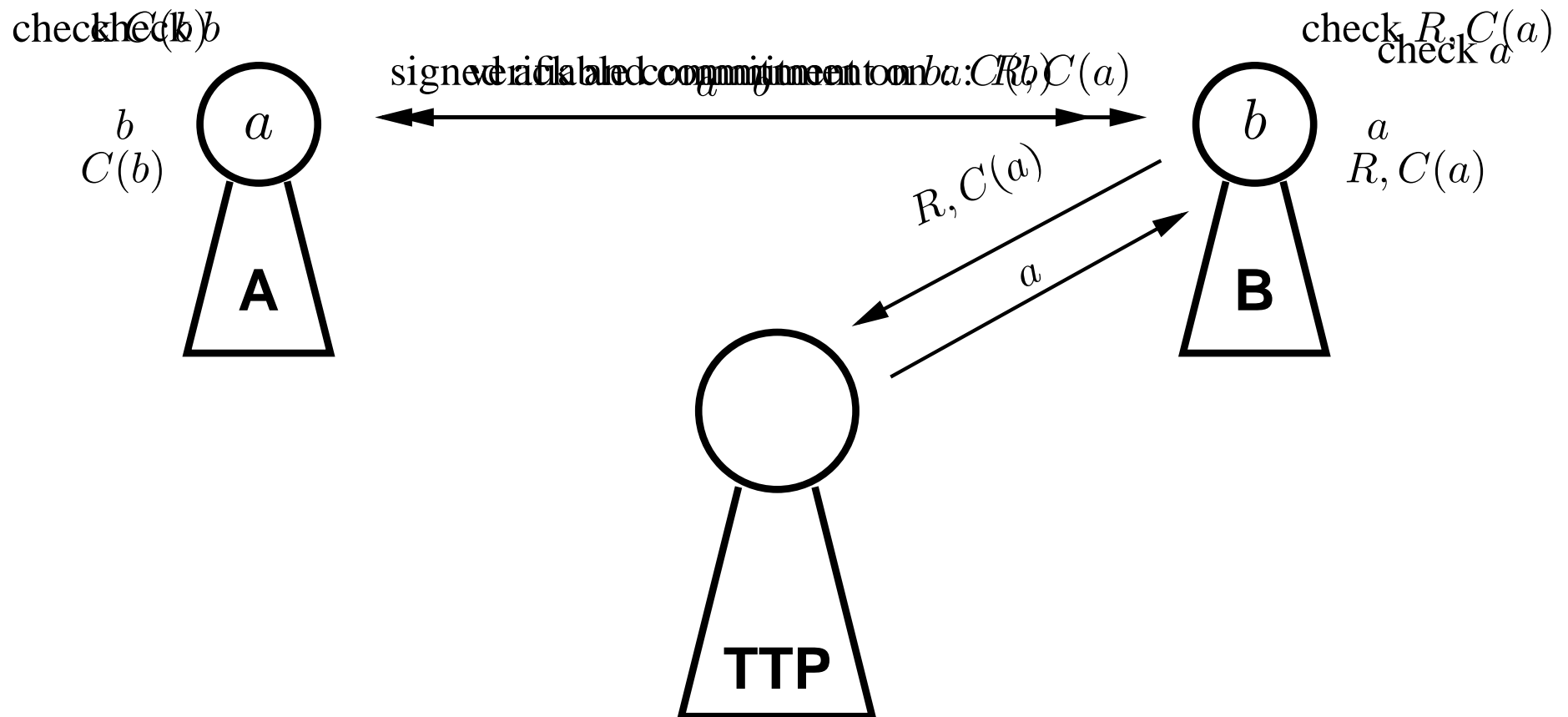
- Validation of fair exchange properties is easy.
- TTP must be **trusted and available**.



## Optimistic Fair Exchange [Asokan et al. 1998]

- TTP can become a bottleneck: only use TTP if something goes wrong.
- Need special item properties to design optimistic protocols:
  - **Revocability**: One item must be revocable by the TTP (e.g., an electronic payment).
  - **Generatability**: One item must be generatable by the TTP (e.g., a software package deposited by the TTP).
- Idea: parties send a commitment first, which can be used by the TTP to resolve the exchange in case of a failure.
- **Cryptography** comes in here:
  - Challenge: how apply cryptography in the right way so that nobody can cheat?

# Interaction Pattern of Optimistic Fair Exchange

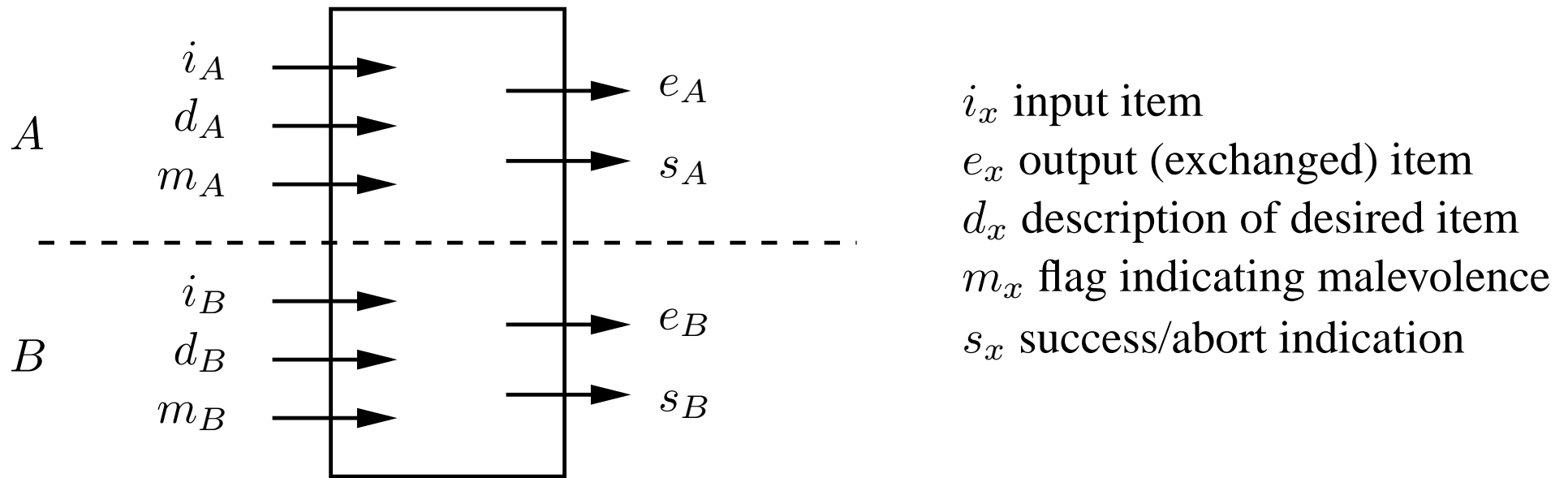


## Why is this fair?

- Two **dangerous cases** can arise:
  - (shown in previous figure)  **$A$  may refuse to send  $a$  after receiving  $b$ :**
    - \* Danger:  $A$  has  $b$  but  $B$  does not have  $a$ .
    - \*  $B$  can prove (through  $R$ ) that  $B$  has followed the protocol.
    - \* TTP can generate  $a$  on behalf of  $B$  (using  $C(a)$ ).■
  - **$B$  may refuse to send  $b$  after receiving  $R, C(a)$ :**
    - \* Danger:  $B$  has all it needs to resolve the protocol and hence get  $a$ .
    - \*  $A$  can request an abort of the exchange at the TTP.
    - \* Such a request can block the TTP from resolving the exchange for  $B$ .
    - \* In case  $B$  was faster,  $B$  must deposit  $b$  at the TTP, and hence TTP can generate  $b$  on behalf of  $A$ .■
- This is a tricky business and we would like to have some formal methods help increase confidence.
- How formalize fairness?

## How Formalize Fairness?

- Let's use trace-based concepts from program verification!



- Assume: the protocol ends for a party  $X$  by **writing something to  $e_X$**  (initially  $\perp$ ). Can write  $e_X$  **at most once**.
- Malevolent parties “try as hard as they can” before doing this.

## Fairness Definitions

- In the following: assume **items match description**.
- First attempt: fairness as an “always safe” **invariant**.

$$\Box(e_A = i_B \Leftrightarrow e_B = i_A)$$

– Problem with atomicity (messages take time).

- Second attempt: fairness as **postcondition** (based on termination state).

$$\Box[(e_A \neq \perp \wedge e_B \neq \perp) \Rightarrow (e_A = i_B \wedge e_B = i_A)]$$

- This is the standard approach [[Chadha et al. 2001](#); [Shmatikov and Mitchell 2002](#)] in formal verification.
- Definition depends on the assumptions about misbehaving parties (we require a misbehaving party to do something, it is not an “interface definition”).

## Fair Exchange vs. Consensus

- Is fair exchange a transaction?
- Define the **two-party misbehavior-tolerant consensus problem**:
  - Two parties **propose** a value  $v \in \{0, 1\}$  and can **decide** on a value.
  - If both parties are well-behaved and decide, their decision is the same.
  - The decision value must be a proposed value.
  - Every well-behaving party eventually decides a value.
- Assume we have a primitive

$$e_A := \text{fair\_exchange}(i_A, d_A)$$

**Can we implement** a distributed primitive

$$\delta := \text{consensus}(\pi)$$

for two-party consensus?

## The Transformation

```

function consensus( $\pi \in \{0, 1\}$ ) returns  $\delta \in \{0, 1\}$ 
  local variable  $t \in \{0, 1, \text{"aborted"}\}$ 
begin
   $t := \text{fair\_exchange}(\pi, \text{desc}(\pi));$             $\{ * \text{ settings a and b from below } * \}$ 
  if  $t \neq \text{"aborted"}$  then return  $\pi;$ 
   $t := \text{fair\_exchange}(\pi, \text{desc}(\neg\pi));$         $\{ * \text{ settings c and d from below } * \}$ 
  if  $t \neq \text{"aborted"}$  then return  $0;$         $\{ * \text{ or 1 consistently } * \}$ 
  return  $\pi;$                                       $\{ * \text{ settings e and f from below } * \}$ 
end

```

setting	a	b	c	d	e	f
$A$	1	0	0	1	0	1
$B$	1	0	1	0	m	m
$\delta$	1	0	0	0	0	1

## Fair Exchange vs. Consensus (cont.)

- Hence: Fair exchange is **at least as hard to solve** as consensus.
  - If consensus is impossible, then so is fair exchange.
- Misbehavior is indistinguishable from a crash (in one instance of fair exchange).
  - Impossibility result of **Fischer, Lynch, and Paterson [1985]** holds.
  - Corollary: There is no asynchronous two-party fair exchange protocol.
- Same impossibility result as on slide **7**, but **Even and Yacobi [1980]** also cover the synchronous case:
  - There are synchronous two-party consensus protocols, but there are no synchronous two-party fair exchange protocols.
  - Fair exchange seems to be harder than consensus.



## Fair exchange vs. Transactions

- Addition of a TTP is a **strong assumption** which helps make life much easier.
  - Consensus (even Byzantine agreement) is trivially solvable using a TTP.
  - Transformation on slide **15** implicitly postulates a TTP.
- In consensus or atomic commitment protocols there is usually a (distinguished) **coordinator process** which ensures unanimity.
  - In consensus this can be one of the participating parties.
  - In fair exchange, this must be an external party (secrecy of items must be preserved).
- Intuition: fair exchange is a kind of **secure transaction**.

## Research Issues

- Fair exchange is a **good candidate** for people coming from the database or consensus world to study security (“the next step”).
  - “Secure” consensus is more than Byzantine agreement.
- **Asymmetry in fair exchange** (due to secrecy).
  - Maybe we need to adapt the consensus definition to be amendable for better comparison?
  - Maybe we need to leave the domain of the usual trace-based formalizations?
- **Recent work** in the area goes in different directions:
  - Use trusted hardware to implement a low-cost, low-latency TTP [[Vogt et al. 2003](#)].
  - Abuse-free fair exchange [[Garay and MacKenzie 1999](#)].
  - Formal analysis [[Buttyán and Hubaux 2001](#)].

# Summary

- Fair exchange is a **fundamental building block** in modern e-commerce.
- Fair exchange is a **difficult and costly task** since it (usually) involves a (costly) trusted third party.
  - Optimistic protocols help.
- **Relation to consensus and transactions** does not seem to be entirely clear.■

Researchers in consensus: drop everything else and work on this!

# Acknowledgements

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## References

- ASOKAN, N., SHOUP, V., AND WAIDNER, M. 1998. Asynchronous protocols for optimistic fair exchange. In *Proceedings of the IEEE Symposium on Research in Security and Privacy* (May 1998), pp. 86–99. Printed version contains some errors. Errata sheet is distributed together with the electronic version.
- BUTTYÁN, L. AND HUBAUX, J.-P. 2001. Rational exchange – A formal model based on game theory. In *Electronic Commerce – WELCOM 2001*, Volume 2232 of *Lecture Notes in Computer Science* (Heidelberg, Nov. 2001), pp. 114–126. Springer-Verlag.
- CHADHA, R., KANOVICH, M., AND SCEDROV, A. 2001. Inductive methods and contract-signing protocols. In P. SAMARATI Ed., *Proceedings of the 8th ACM Conference on Computer and Communication Security* (Philadelphia, PA, Nov. 2001), pp. 176–185. ACM Press.
- DOLEV, D. AND YAO, A. C. 1983. On the security of public key protocols. *IEEE Transactions on Information Theory* 29, 2 (March), 198–208.
- EVEN, S. AND YACOBI, Y. 1980. Relations among public key signature systems. Technical Report 175, Computer Science Department, Technicon, Haifa, Israel.
- FISCHER, M. J., LYNCH, N. A., AND PATERSON, M. S. 1985. Impossibility of distributed consensus with one faulty process. *Journal of the ACM* 32, 2 (April), 374–382.

- GARAY, J. A. AND MACKENZIE, P. 1999. Abuse-free multi-party contract signing. In *Distributed Computing – DISC '99*, Volume 1693 of *Lecture Notes in Computer Science* (Bratislava, Slovak Rep., 27–29 Sept. 1999), pp. 151–165. Springer-Verlag.
- SHMATIKOV, V. AND MITCHELL, J. C. 2002. Finite-state analysis of two contract signing protocols. *Theoretical Computer Science* 283, 2, 419–450.
- VOGT, H., GÄRTNER, F. C., AND PAGNIA, H. 2003. Supporting fair exchange in mobile environments. *ACM/Kluwer Journal on Mobile Networks and Applications (MONET)* 8, 2 (April).

## Additional Slides

## Extendible Consensus

- Adapt definition of consensus to an “extendible” set of processes.
- Define: set of processes  $\Pi = \{p_1, p_2, \dots, p_n\}$ .
- Separate  $\Pi$  into  $\Pi_a$  and  $\Pi_b$  such that
  - $\Pi_a \subseteq \Pi$  and  $\Pi_b \subseteq \Pi$
  - $\Pi_a \cap \Pi_b = \emptyset$
- Define extendible consensus as follows:
  - For processes in  $\Pi_a$  (uniform) consensus must hold.
  - For processes in  $\Pi_b$ :
    - \* When a process  $p \in \Pi_b$  decides, then this must be the value decided by the processes in  $\Pi_a$ .
- Intuition: processes in  $\Pi_b$  can join in on demand.